

Atomic-Scale Structure of Biogenic Materials by Total X-ray Diffraction: A Study of Bacterial and Fungal MnO_x

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Currently, technology is looking for smaller scale, ordered materials with well-defined properties. Nanophase materials are, therefore, being manufactured in increasing numbers.^{1–3} Nature is also a prolific producer of nanophase materials. A typical example of this is the microorganism assisted, or biogenic, oxidation of water-soluble metal ions into insoluble oxides.⁴ Indeed this process has been taking place for millions of years leaving its signature all around: in the sediments on the ocean floor and in the soil on land. Nature's evident success is inspiring and scientists are trying to employ its tools for applications including manufacturing of magnetic nanoparticles⁵ and capturing of contaminant metal ions.^{6–8} Thus understanding the way living microorganisms produce materials, in particular nanophase metal oxides, is becoming important not only for the advance of today's technology but also for remediating some of its unwanted consequences such as metal pollution.

One of the most important prerequisites to understanding a physicochemical process, such as the formation of a nanophase material, is the knowledge of the atomic-scale structure of its product. Recently, good progress has been made in determining the structure of synthetic (i.e., man-made) nanophase materials by employing total X-ray diffraction (XRD) involving a combination of high-energy XRD and atomic pair distribution function (PDF) analysis.^{9–11} This nontraditional approach has also been applied to nanophase materials of geological interest, such as ores.¹² The approach can also be applied to mate-

ABSTRACT Biogenic materials are produced by microorganisms and are typically found in a nanophase state. As such, they are difficult to characterize structurally. In this report, we demonstrate how high-energy X-ray diffraction and atomic pair distribution function analysis can be used to determine the atomic-scale structures of MnO_x produced by bacteria and fungi. These structures are well-defined, periodic, and species-specific, built of $\text{Mn}-\text{O}_6$ octahedra forming birnessite-type layers and todorokite-type tunnels, respectively. The inherent structural diversity of biogenic material may offer opportunities for practical applications.

KEYWORDS: biogenic materials · structure determination · X-ray diffraction · manganese oxides

rials freshly produced by living microorganisms. As an example we consider MnO_x produced by bacteria and fungi. These biogenic materials show a length of structural coherence of about 2–3 nm only and, in this sense, are in a nanophase state. Nevertheless, their atomic-scale structure is periodic and can be described in simple crystallographic terms. Surprisingly the crystal structures of fungal and bacterial MnO_x turn out to be substantially different indicating that biogenic materials are inherently structurally diverse.

Manganese oxides are ubiquitous in nature¹³ and have been used by mankind for many thousands of years—first as pigments and today as catalysts and battery materials. This has generated a long-lasting interest in their genesis. Several studies on MnO_x produced by microorganisms have been carried out but no complete structural determination has yet been performed. The studies have only suggested that bacterial MnO_x is likely to possess a layered-type structure of the type found in the mineral birnessite.^{14,15} Even less is known about fungal MnO_x .^{16,17}

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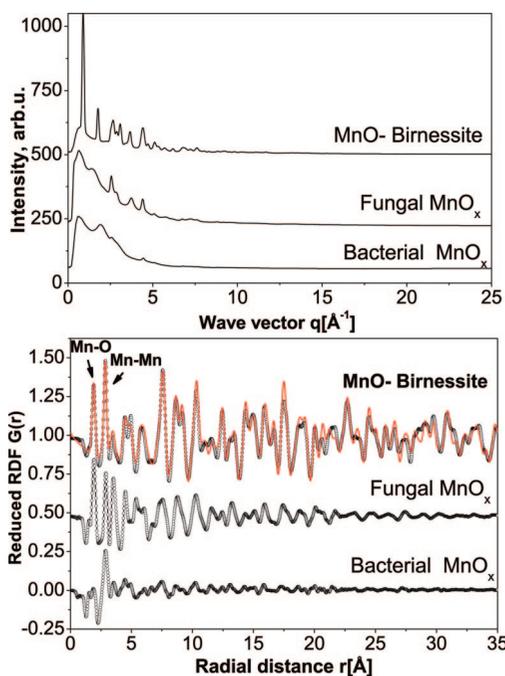


Figure 1. Experimental XRD patterns (upper part) and the corresponding atomic PDFs for crystalline, fungal, and bacterial MnO_x . PDF peaks reflecting first neighbor Mn–O and Mn–Mn correlations are marked with arrows. A model PDF (line in red) based on the structure of hexagonal birnessite is shown as well.

Traditionally the three-dimensional (3D) structure of materials is determined by measuring and analyzing the positions and intensities of the Bragg peaks in their XRD patterns.¹⁸ Traditional (*i.e.* Bragg) XRD studies of biogenic materials are possible¹⁹ but are difficult and are often imprecise. The reason is that biogenic materials are usually highly dispersed and/or of very low crystallinity, often contain water and, as such, show diffraction patterns with a very few, if any, Bragg peaks and a pronounced diffuse component (see Figure 1). Spectroscopy techniques like XANES/EXAFS are also widely used for structural characterization of materials. For biogenic materials, spectroscopy techniques may deliver important information about the valence state of metal ions and their immediate coordination, but are not capable of elucidating the atomic ordering beyond 5–6 Å (*e.g.*, see Figure 1 in Kim *et al.*²⁰). Total XRD is well suited to study materials structured at the nanoscale, as demonstrated recently.^{9–11,21}

RESULTS AND DISCUSSION

Biogenic MnO_x studied here were produced by *L. dis-cophora* SP-6 bacteria¹⁵ and fungi from the *Acremonium strictum* family.²² High-energy XRD patterns for bacterial, fungal, and crystalline MnO_2 (birnessite) standard are shown in Figure 1 (the upper part). Sharp Bragg peaks are present in the XRD pattern for synthetic birnessite, as can be expected for a material of good crystallinity. The XRD patterns for both bacterial and fungal MnO_x , however, show only a few broad Bragg-like peaks. Such dif-

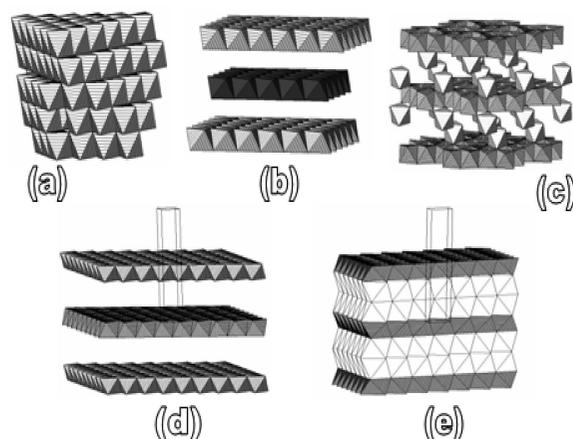


Figure 2. Fragments from the structures of manganese oxide (a), lithiophorite (b), chalcophanite (c), birnessite (d), and birnessite-like “slabs” of Mn–O₆ octahedra separated by regions scarcely populated with Mn ions and water (lightly shaded) (e). The unit cells in birnessite and bacterial MnO_x are outlined with thin solid lines.

fuse diffraction patterns are very difficult to analyze by traditional approaches. When considered in real space, in terms of the corresponding atomic PDFs however, they lend themselves to structure search and refinement.²¹ The experimental PDFs $G(r) = 4\pi r[\rho(r) - \rho_0]$, where $\rho(r)$ and ρ_0 are the local and average atomic number density, respectively, extracted from the XRD patterns are also shown in Figure 1 (the bottom part). As can be seen in the figure the $G(r)$ for birnessite exhibits a series of well-defined peaks to high real-space distances reflecting the presence of a long-range, periodic, atomic ordering. The experimental data can be approximated well in terms of a structure model based on a periodic, hexagonal type lattice (space group, $P6_3/mmc$) with parameters $a = 2.84(1)$ Å and $c = 14.02(1)$ Å, and Mn at (0,0,0) and oxygen at 2/3, 1/3, 0.07 positions inside the unit cell. The structure features layers of edge sharing Mn–O₆ octahedra, as shown in Figure 2. The excellent level of agreement between the present and previous literature data²³ for the crystal structure of birnessite demonstrate the fact that atomic PDFs very accurately reflect the 3D atomic ordering in materials.

As can be seen in Figure 1 the PDFs for both biogenic manganese oxides too show several well-defined peaks but they decay to zero faster (*i.e.*, already at 2–3 nm) than those in the PDF for synthetic birnessite, reflecting the limited length of structural coherence in the former materials. The first peak in the PDFs for biogenic MnO_x is positioned at approximately 1.9 Å and the second at approximately 2.85 Å. The first two peaks in the PDF for polycrystalline birnessite are positioned at the same distances. Here they reflect the first neighbor Mn–O and Mn–Mn atomic pairs from edge sharing Mn–O₆ octahedra, respectively. The similarity between the low- r parts of the experimental PDFs in Figure 1 indicates that biogenic MnO_x studied here, like synthetic birnessite, are built up from intercon-

nected Mn–O₆ octahedra. This conclusion would have been difficult to arrive at if the XRD patterns and not their Fourier transforms, the atomic PDFs, had been considered alone. The higher-*r* parts (*i.e.*, above 5–6 Å) of the experimental PDFs in Figure 1, however, are dissimilar and demonstrate that the longer-range atomic ordering, that is, the way the Mn–O₆ octahedral units connect together and fill up the space, is distinctly different in the three different manganese oxides studied. Such a conclusion is difficult to arrive at on the basis of spectroscopy (*e.g.*, EXAFS) data alone.

To reveal the 3D structure of biogenic MnO_x we tested several structural models as follows: In line with the suggestions of previous studies^{14,15} the PDF for bacterial MnO_x was approached with models featuring layers of Mn–O₆ octahedra. As such we considered the structures of lithiophorite, chalcophanite, and hexagonal and triclinic birnessite (see Figure 2) that occur in MnO_x minerals. As shown in Figure 2 lithiophorite may be viewed as a stack of alternating layers of octahedra, perfect and defect (dark shaded in Figure 2), with the latter layers having 33% of their octahedral sites vacant. Chalcophanite also features layers of edge-sharing Mn–O₆ octahedra. Here one in seven of the octahedral sites in each of the Mn layers is vacant and the “capping units” (lightly shaded in Figure 2) are positioned exactly above and below the vacancies. Birnessite is a stack of layers of edge-sharing Mn–O₆ octahedra where approximately one in six of the cation sites are vacant. The “missing” Mn cations are positioned between the layers, just above or below the vacant sites. As can be seen in Figure 3 none of those models adequately reproduce the experimental data. The agreement improved when (i) water was introduced between the layers and (ii) the number of vacant metal sites in the layers was increased. Such a model featuring birnessite-type layers where about 30% of the metal sites are vacant and the “missing” Mn cations have migrated into the interlayer space was indeed able to reproduce the experimental PDF data in good detail, as can be seen in Figure 3. This model structure of bacterial MnO_x may be described well in terms of a triclinic lattice (space group *P1*) with parameters $a = 2.832(5)$ Å, $b = 2.866(5)$ Å, $c = 12.6(5)$ Å and $\alpha = 89.3(2)$, $\beta = 90.5(5)$, and $\gamma = 125.6(5)^\circ$. The coordinates of the individual atomic species inside the unit cell are given in the Supporting Information. The refined chemical formula of the material is $\{Mn_{0.3}\} \cdot [Mn_{0.7-0.3}]O_2 \cdot (H_2O)_{5.5}$. Here □ represents the vacant metal positions in the layers of Mn–O₆ octahedra, that is equal to the number of interlayer manganese, {Mn}, ions. The relatively high concentration of interlayer {Mn}, and associated layer vacancies, is consistent with an average Mn oxidation state lower than +4 in bacterial MnO_x, as found by XANES.¹⁵

The interlayer {Mn} atoms sit on both sides of the layers and share oxygen atoms from both the [Mn–O] layers and the water molecules positioned in between

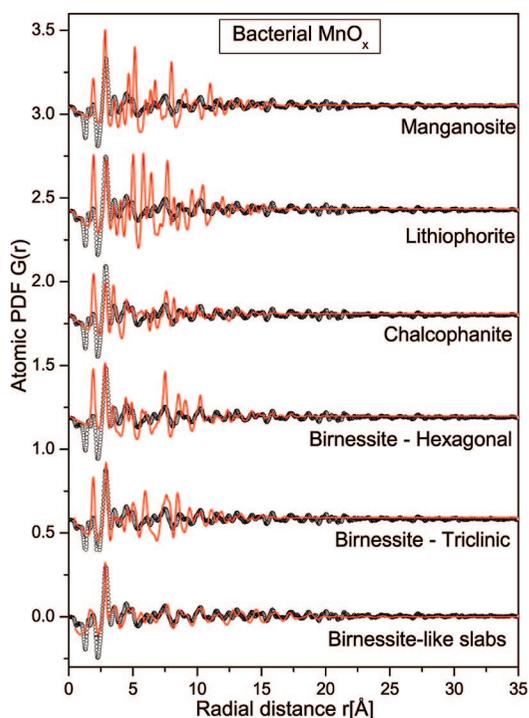


Figure 3. Experimental (symbols) and model (lines in red) atomic PDFs for bacterial MnO_x. The models are based on the structures of the MnO_x minerals listed in the plot. The low-*r* part of the data is given in the Supporting Information on an enlarged scale.

these layers. Thus the oxygen coordination of all Mn atoms in bacterial MnO_x appears to be octahedral and the whole material may be viewed as a highly defective “network” of both edge and corner-sharing Mn–O octahedra as shown in Figure 2e. The network resembles vaguely that of manganosite (Figure 2a) but in contrast to this material, it exhibits a very nonuniform distribution of Mn atoms that tend to “cluster” into birnessite-type “slabs” (70% of all Mn atoms) that are spaced by regions less populated with metal ions (lightly shaded octahedra in Figure 2e). It is in these interlayer regions where water resides. Indeed, according to our study, there are about 5.5 water molecules per Mn atom in bacterial MnO_x. This relatively high water content is consistent with the fact that this biogenic material was formed in an aqueous medium.¹⁵

As can be seen in Figures 1 and 4, the experimental PDF for fungal MnO_x has a very strong third peak at about 3.45 Å. This is the typical separation between Mn atoms from octahedra that are connected through their vertices. Neither the PDF for birnessite nor that for bacterial MnO_x shows such a strong peak. This observation indicates that the ratio of edge to corner sharing octahedra in fungal MnO_x is different from that seen in layered manganese oxides. This prompted us to look for other types of model structures. As such we considered tunnel-type structures that too are often found in MnO_x minerals. Fragments of the structure models we tested are shown in Figure 5. They included a pyrolusite-type model featuring a dense 3D framework of edge and corner sharing Mn–O₆ octa-

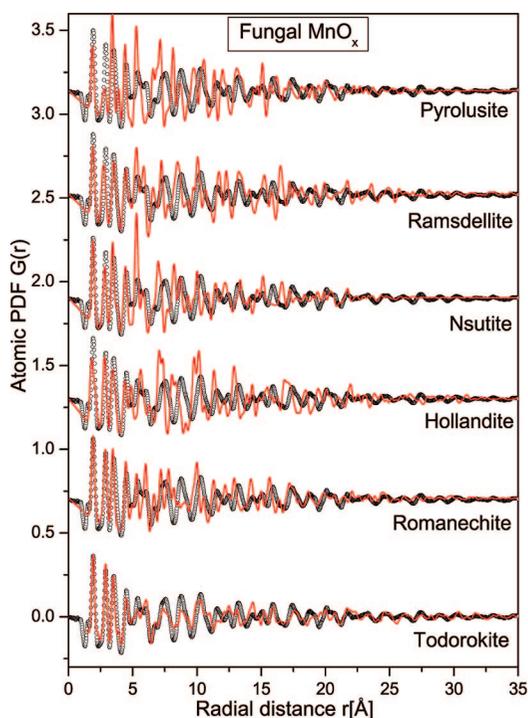


Figure 4. Experimental (symbols) and model (lines in red) atomic PDFs for fungal MnO_x . The models are based on the structures of manganese oxide minerals listed in the plot. The low- r part of the data is given in the Supporting Information on an enlarged scale.

hedra, a ramsdellite-type model featuring a framework of $\text{Mn}-\text{O}_6$ units having tunnels that are 1×2 octahedra on a side, an nsutite-type model featuring a framework of $\text{Mn}-\text{O}_6$ units having tunnels that are 1×3 and 3×3 octahedra on a side, a hollandite-type model featuring a framework of $\text{Mn}-\text{O}_6$ units having tunnels with square cross sections measuring 2×2 octahedra on a side, a romanechite-type model featuring a framework of $\text{Mn}-\text{O}_6$ units having tunnels that are 2×3 octahedra on a side, and a todorokite-type model featuring a framework of $\text{Mn}-\text{O}_6$ units having tunnels that are 3×3 octa-

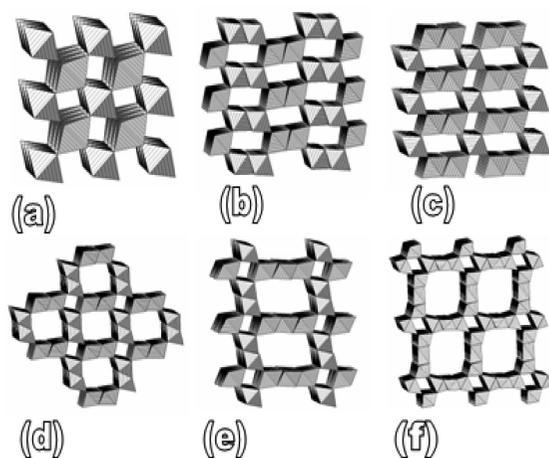


Figure 5. Fragments from the crystal structures of pyrolusite (a), ramsdellite (b), nsutite (c), hollandite (d), romanechite (e), and todorokite (f). The structures feature open frameworks of $\text{Mn}-\text{O}_6$ octahedra.

hedra on a side. As can be seen in Figure 4 the last model performed best. Thus, according our study, the 3D structure of fungal MnO_x may be described well in terms of a monoclinic lattice (space group $P12/M1$) with parameters $a = 9.20(1) \text{ \AA}$, $b = 2.88(1) \text{ \AA}$, $c = 9.92(1) \text{ \AA}$ and $\alpha = 90.0^\circ$, $\beta = 93.52(5)$ and $\gamma = 90.0^\circ$. The refined chemical formula of the material is $[\text{Mn}]_2(\text{H}_2\text{O})_{0.5}$ indicating an average Mn oxidation state of +4. The water content in fungal MnO_x is lower than that found in bacterial MnO_x and is consistent with the fact that the fungal MnO_x formed in a drier medium.²² The coordinates of the individual atoms inside the monoclinic unit cell of fungal MnO_x are given in the Supporting Information.

In summary, our study shows that microorganisms produce materials that are nanophase but with well-defined and periodic atomic-scale structures, and that the resulting structure is species-specific.²⁴ In particular, microorganisms such as *L. discophora* SP-6 bacteria that thrive in aquatic environments and oxidize metal ions relatively quickly (*i.e.*, in minutes to hours) are seen to produce layered-type manganese oxides containing a large number of structural defects, and water. In contrast microorganisms such as *Acremonium strictum* fungi that prefer a less moist environment and oxidize metal ions relatively slowly (*i.e.*, over several days to weeks) are seen to produce tunnel-type manganese oxides that are almost defect-free. Obviously the structure of many materials of biogenic origin, such as deposits, sediments, and ores takes shape at very early stages of their formation, that is, during the oxidation of water-soluble metal ions into nanophase oxides. Given the great diversity of microorganisms that have lived on Earth, it is not difficult to understand why MnO_x of biogenic origin occurs in more than 30 different structure types.¹³

The structural diversity of biogenic materials is not just of academic interest. This seemingly inherent property of biogenic materials may be useful in technological applications. For example, nanophase metal oxides of a particular structure type, and hence particular properties (magnetic, absorptive, catalytic, *etc.*), may be harvested in a laboratory by choosing an appropriate microorganism and environment, as already demonstrated by Prozorov *et al.*⁵ In a given environment (*e.g.*, industrial, mining, *etc.*) a particular type of microorganism may be looked for and chosen over others so that trace metal ions are captured and retained in a material with a more rigid (*e.g.*, dense network) structure. The success of the efforts along these lines will depend on the ability to determine the atomic-scale structure of biogenic materials not only in detail but in terms (*e.g.*, see the Supporting Information) allowing convenient computation and prediction of their properties. Indeed any systematic studies on water soluble metal ions, including verification and refinement of Pourbaix-type diagrams,²⁵ would benefit from the ex-

perimental approach demonstrated here. Total XRD can tackle such nontrivial tasks with success.

METHODS

Materials Preparation. Bacterial MnO_x studied here was produced by growing a liquid culture of *L. discophora* SP-6 to a stationary phase at room temperature. The resulting MnO_x was of a fibrillar morphology and with dimensions of the order of 10 nm wide and 10 nm long.¹⁵ Fungal MnO_x studied here was produced by a fungus of the *Acremonium strictum* family, in particular KR21-2 strain.^{16,17} Since KR21-2 repeatedly failed to produce MnO_x in liquid media a solid agar medium was used. The oxide was grown at room temperature and appeared as particles of an oblong plate morphology, several hundred nanometers to one micrometer in size.²²

X-ray Diffraction Studies. High-energy XRD experiments were carried out at the beamline 11IDC at the Advanced Photon Source, Argonne National Laboratory using X-rays of energy 115.232 keV ($\lambda = 0.1076 \text{ \AA}$) and a large area (mar345) detector. Fresh samples of biogenic MnO_x were sealed in glass capillaries and data taken at room temperature. Synthetic crystalline MnO₂ powder (birnessite) was also measured and used as a standard.

Atomic PDFs Data Analysis and Structure Modeling. The processing of the raw XRD data and derivation of atomic PDFs was done with the help of the program RAD.²⁶ The test and refinement of structure models was done with the help of the program PDFFIT.²⁷

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Supporting Information Available: Structure data for fungal and bacterial MnO_x. This material is available free of charge via the Internet at <http://pubs.acs.org>.

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