Synthesis, structure and properties of Pb$_2$CuB$_2$O$_6$

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Received 7 December 2005; accepted 23 December 2005

Available online 26 January 2006

Abstract

Single crystals of Pb$_2$CuB$_2$O$_6$ were grown from a PbO/CuO/B$_2$O$_3$ flux, and crystallize in a monoclinic cell of dimensions $a = 5.6311(6)$, $b = 8.7628(9)$, $c = 6.2025(6)$ Å, and $\beta = 115.7060(10)^\circ$ with $Z = 2$; the space group is $P2_1/c$ (no. 14). The structure was determined from 662 unique reflections and refined to the final residuals $R_1 = 0.0217$, $wR_2 = 0.0586$. The structure is characterized by the two-dimensional layer of interconnected rectangular planar CuO$_4$ and triangular planar BO$_3$ groups. The results of quantitative analysis ICP, DTA, vibrational spectroscopy, and magnetic investigations are also presented.

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Keywords: C. X-ray diffraction; A. Oxide; B. Crystal growth; D. Crystal structure; D. Magnetic properties

1. Introduction

One of the primary goals of chemistry is the development and creation of new materials, and the growth of single crystals from oxide fluxes is a good way to facilitate the discovery of new compounds. Synthesis of complex oxides and the improvement of existing technologies for the production of these materials are based on the fundamental investigations into the relationship between composition, structure, and properties.

Owing to their potentially interesting properties, complex oxides such as cuprates and borates are of interest. For example, cuprate compounds such as SrCu$_2$O$_3$ [1,2], Sr$_{14}$Cu$_{24}$O$_{41}$ [3], and La$_4$Cu$_3$MoO$_{12}$ [4,5] have attracted attention because of their unusual low-temperature magnetic properties. Cuprate and borate groups are two-dimensional spin gap systems with the exact dimer ground state [6–8]. Additionally, several borate phases display excellent linear and non-linear optical properties [9–16]. The combination of cuprate and borate groups in the same compound may generate a new class of interesting materials as the ternary PbO–CuO–B$_2$O$_3$ system has been studied very little [17]. In this report, the synthesis, crystal structure, DTA, vibrational spectroscopy, and magnetic properties of Pb$_2$CuB$_2$O$_6$ are described, which is the first of a new family of lead copper borates in the ternary system PbO–CuO–B$_2$O$_3$ that have been discovered.

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2. Experimental

2.1. Polycrystalline synthesis

A polycrystalline sample of Pb$_2$CuB$_2$O$_6$ was prepared by standard solid-state reaction method using PbO (99.99%, Alfa-Aesar), CuO (99.995%, Alfa-Aesar), and B$_2$O$_3$ (99.98%, Sigma–Aldrich) as the starting components in the molar ratio 2:1:1. The reagents were mixed, ground in an agate mortar, and packed into a platinum crucible. The mixture was heated to 773 K in air for 24 h (with occasional grinding), and then sintered at 923 K for an additional 24 h. The sample purity was verified by X-ray powder diffraction. The chemical equation can be expressed as follows:

$$2\text{PbO} + \text{CuO} + \text{B}_2\text{O}_3 \rightarrow \text{Pb}_2\text{CuB}_2\text{O}_6$$

2.2. Single crystal synthesis

A 30 g polycrystalline sample was melted in a platinum crucible at 1173 K, and kept at 1173 K for 8 h. The furnace was slowly cooled to 953 K at a rate of 0.1 K/min, and then cooled to room temperature at a rate of 20–30 K/h. Dark green needle-like crystals were separated from the crucible for the structure determination.

2.3. Large single crystal growth

In order to obtain crystals for property measurements, crystal growth was carried out in a vertical Molysili furnace. The polycrystalline sample with 120 g was melted in a platinum crucible at 1173 K, kept at 1173 K for 12 h. A platinum wire was dipped into the solution and the furnace was slowly cooled to 953 K at a rate of 0.3 K/h. The sample was then cooled down to room temperature at a rate of 20–30 K/h. The crystals were cracked, but parts of them were transparent and useful for the properties measurement.

2.4. X-ray powder diffraction

X-ray powder diffraction analysis of Pb$_2$CuB$_2$O$_6$ was performed at room temperature in the angular range of $2\theta = 10$–70° with a scan step width of 0.02° and a fixed counting time of 1 s/step using an automated Rigaku X-ray diffractometer equipped with a diffracted-beamed monochromator set for Cu Kα ($\lambda = 1.5418$ Å) radiation. The X-ray powder diffraction patterns of both the synthesized and calculated Pb$_2$Cu(BO$_3$)$_2$ are identical (Fig. 1), indicating that the synthesized phase contains no other phases.

2.5. X-ray crystallography

A needle-shaped blue single crystal of Pb$_2$CuB$_2$O$_6$ with dimensions 0.02 mm \(\times\) 0.02 mm \(\times\) 0.70 mm was chosen for the structure determination. Unit cell parameters were derived from a least-squares analysis of 2418 reflections in

![Fig. 1. X-ray powder diffraction patterns of both the synthesized and calculated Pb$_2$CuB$_2$O$_6$. The red curve is its calculated pattern, the black one is its synthesized pattern.](image-url)
Table 1
Crystal data and structure refinement for Pb$_2$CuB$_2$O$_6$

<table>
<thead>
<tr>
<th>Property</th>
<th>Value</th>
</tr>
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<tbody>
<tr>
<td>Empirical formula</td>
<td>Pb$_2$CuB$_2$O$_6$</td>
</tr>
<tr>
<td>Formula weight</td>
<td>595.54</td>
</tr>
<tr>
<td>Temperature (K)</td>
<td>153(2)</td>
</tr>
<tr>
<td>Crystal system</td>
<td>Monoclinic</td>
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<tr>
<td>Space group</td>
<td>P2$_1$/c</td>
</tr>
<tr>
<td>Unit cell dimensions</td>
<td></td>
</tr>
<tr>
<td>a</td>
<td>5.6311(6) Å</td>
</tr>
<tr>
<td>b</td>
<td>8.7628(9) Å</td>
</tr>
<tr>
<td>c</td>
<td>6.2025(6) Å</td>
</tr>
<tr>
<td>Volume (Å$^3$)</td>
<td>275.77(5)</td>
</tr>
<tr>
<td>Density (calculated; g/cm$^3$)</td>
<td>4.02–28.54</td>
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<tr>
<td>Absorption coefficient (mm$^{-1}$)</td>
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</tr>
<tr>
<td>F(0 0 0)</td>
<td>502</td>
</tr>
<tr>
<td>Theta range for data collection (°)</td>
<td>-7 ≤ h ≤ 7, -11 ≤ k ≤ 11, -8 ≤ l ≤ 8</td>
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<td>Index ranges</td>
<td>2418</td>
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<tr>
<td>Reflections collected</td>
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<tr>
<td>Independent reflections</td>
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</tr>
<tr>
<td>Completeness to θ = 27.19</td>
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</tr>
<tr>
<td>Maximum and minimum transmission</td>
<td>0.3219 and 0.2172</td>
</tr>
<tr>
<td>Data/restraints/parameters</td>
<td>662/0/53</td>
</tr>
<tr>
<td>Goodness-of-fit on F$^2$</td>
<td>1.17</td>
</tr>
<tr>
<td>Final $R$ indices $[F^2 &gt; 2\sigma(F^2)]^a$</td>
<td>$R_1 = 0.0217, wR_2 = 0.0586$</td>
</tr>
<tr>
<td>$R$ indices (all data)</td>
<td>$R_1 = 0.0226, wR_2 = 0.0591$</td>
</tr>
<tr>
<td>Extinction coefficient</td>
<td>0.0016(5)</td>
</tr>
<tr>
<td>Largest diffraction peak and hole (eÅ$^{-3}$)</td>
<td>2.19 and -2.2</td>
</tr>
</tbody>
</table>

$^a R_1 = \sum|F_{o}| - |F_{c}|/\sum|F_{o}|$ and $wR_2 = \sqrt{\sum w(F_{o}^2 - F_{c}^2)^2/\sum wF_{o}^4}^{1/2}$ for $F_{o}^2 > 2\sigma(F_{o}^2)$ and $w^{-1} = \sigma^2(F_{o}^2) + (0.035P)^2 + 1.3590P$ where $P = (F_{o}^2 + 2F_{c}^2)/3$.

the range 4.02° < θ < 28.54° on a Bruker SMART – 1000 CCD diffractometer using monochromatic Mo Kα radiation ($\lambda = 0.71073$ Å) and integrated with the SAINT – Plus program [18]. All calculations were performed with programs from the SHELXTL crystallographic software package [19]. The systematic absences $h 0 l$, $l = 2n + 1$, and $0 k 0$, $k = 2n + 1$ unambiguously define the space group P2$_1$/c for the compound Pb$_2$CuB$_2$O$_6$. The positional parameters for the Pb and Cu atoms were determined from the direct methods with the remaining atomic positions determined from analysis of subsequent difference electron density syntheses. A face-indexed absorption correction was performed numerically using the XPREP program, followed by the SADABS program [20]; equivalent reflections were then averaged. Final least-squares refinement on $F^2$ with data having $F^2 > 2\sigma(F^2)$ includes anisotropic displacement parameters for all atoms. The final difference Fourier synthesis may have shown maximum and minimum peaks at 2.19 (1.08 Å from Pb$_1$) and -2.26 eÅ$^{-3}$ (0.82 Å from Pb$_1$), respectively. Additional crystal data and experimental conditions are summarized in Table 1.

2.6. Quantitative analysis

The composition of the new compound Pb$_2$CuB$_2$O$_6$, with respect to the elements lead, copper, and boron, was verified using ICP on a VISTA–MPX Spectrometer.

2.7. Vibrational spectroscopy

IR spectroscopy was carried out with the objective of specifying and comparing the coordination of boron in Pb$_2$CuB$_2$O$_6$. Its mid-infrared spectrum was obtained at room temperature via a Bio-Rad FTS-60 FTIR spectrometer. The sample was thoroughly mixed with dried KBr (5 mg of the sample, 450 mg of KBr). The spectrum was collected in a range from 400 to 4000 cm$^{-1}$ with a resolution of 2 cm$^{-1}$. At least two spectra for each sample were recorded. Infrared spectra were corrected for the dark current noises and background using the two-point baseline correction.
Each spectrum was normalized by making its absorption vary from zero to one arbitrary unit. Such normalization was necessary to eliminate the concentration effect of the powder sample in the KBr disc.

2.7.1. Thermoanalytical investigations
Thermal stability of Pb$_2$CuB$_2$O$_6$ was examined under static air with a differential thermal analyzer 1600–2910 DSC. The sample and reference (Al$_2$O$_3$) were enclosed in Pt crucibles, heated, and then cooled at a rate of 10 K/min.

2.7.2. Magnetic susceptibility
The temperature dependence of the magnetic moment for the polycrystalline, powdered sample of Pb$_2$CuB$_2$O$_6$ was determined on a Quantum Design MPMS5 Superconducting Quantum Interference Device (SQUID) magnetometer in the temperature range 2–300 K. A quantity of 240 mg was enclosed in a cellulose capsule, inserted into a transparent plastic tube, and attached to the sample holder rod. The sample was field cooled (FC) in 500 Oe and zero field cooled (ZFC) before 500 Oe field was applied; in each case the magnetic moment of the sample was measured as the sample was warmed to 300 K. The molar susceptibility for both data sets was obtained by multiplying the magnetic moments by the formula weight (595.54) and dividing by the applied field (500 Oe) and the sample mass (240 mg). These two sets of data were compared for evidence of magnetic order. Additionally, these data were fitted to the Curie–Weiss law so that magnetic parameters could be extracted.

3. Results and discussion

3.1. Crystal structure of Pb$_2$CuB$_2$O$_6$

Final atomic coordinates of the title compound are listed in Table 2. Selected interatomic distances and angles are given in Table 3.

The structure consists of rectangular planar CuO$_4$ units, trigonal–planar BO$_3$ groups, and polyhedral PbO$_7$ units. Fig. 2 displays the structural connectivity along each of the crystallographic axes. The structure is characterized by the two-dimensional layer of interconnected rectangular planar CuO$_4$ and triangular planar BO$_3$ groups as shown in Fig. 2a (view along a axis). These layers extend parallel to the $b$—$c$ plane and the structure is completed by joining successive layers by interleaving Pb atoms. The CuO$_4$ rectangular planes of the sheet are rotated around the O(2)–Cu–O(2) axes out of the $b$—$c$ plane, forming a herringbone pattern when viewed along the c-axis (Fig. 2b). The B atoms bridge the isolated planar CuO$_4$ groups.

The Pb–O distances vary from 2.395(5) to 2.894(4) Å with an average value of 2.699(5) Å. Four of the bond lengths are typical of average Pb–O bond lengths [21,22], while the other three bonds are longer than expected (from 2.769(5) to 2.894(4) Å). If these three longer distances are considered to be a weak-bonding interaction, then the coordination environment around Pb should be described as a distorted seven coordinate polyhedron. The average Cu–O distance of 1.937(5) Å is similar to values observed in other copper borates, e.g., 1.939(3) Å for Ba$_2$Cu(BO$_3$)$_2$ [23] and 1.95(1) Å for Cu$_3$B$_2$O$_6$ [24]. The BO$_3$ groups are quite regular. The average B–O distance, 1.382(9) Å, is similar to interactions observed in a variety of other simple borates [25–27]. All O atoms are bonded to four cations (see Table 4).

Table 2
Atomic coordinates ($\times 10^4$) and equivalent isotropic displacement parameters ($\AA^2 \times 10^3$) for Pb$_2$CuB$_2$O$_6$

<table>
<thead>
<tr>
<th>Atom</th>
<th>x</th>
<th>y</th>
<th>z</th>
<th>U$_{eq}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pb(1)</td>
<td>8026(1)</td>
<td>1075(1)</td>
<td>1575(1)</td>
<td>6(1)</td>
</tr>
<tr>
<td>Cu (1)</td>
<td>5000</td>
<td>5000</td>
<td>0</td>
<td>6(1)</td>
</tr>
<tr>
<td>B(1)</td>
<td>2612(15)</td>
<td>2508(8)</td>
<td>$-3430(12)$</td>
<td>6(1)</td>
</tr>
<tr>
<td>O(1)</td>
<td>208(10)</td>
<td>3227(5)</td>
<td>860(8)</td>
<td>8(1)</td>
</tr>
<tr>
<td>O(2)</td>
<td>4855(10)</td>
<td>3207(5)</td>
<td>1789(8)</td>
<td>9(1)</td>
</tr>
<tr>
<td>O(3)</td>
<td>2572(10)</td>
<td>4056(5)</td>
<td>$-2939(9)$</td>
<td>8(1)</td>
</tr>
</tbody>
</table>

$U_{eq}$ is defined as one-third of the trace of the orthogonalized $U_{ij}$ tensor.
For further clarification, the bond valence sums of each atom in the compound Pb$_2$CuB$_2$O$_6$ are calculated [28,29] and listed in Table 4. These charges, based on the bond lengths determined by the X-ray structure analysis, are in agreement with the expected oxidation states.

4. Composition

The quantitative analysis on a sample of Pb$_2$CuB$_2$O$_6$ using ICP confirms the composition of the new lead copper borate based on the crystal structure solution (theoretical: 69.6% Pb, 10.7% Cu, 3.6% B; experimental: 65.1% Pb, 10.6% Cu, 3.7% B).

4.1. Thermal behavior of Pb$_2$CuB$_2$O$_6$

Samples were heated at 10 K/min to 1173 °C on the DTA; there is a strong signal only at 968 K (Fig. 3), which implies that the Pb$_2$CuB$_2$O$_6$ melts congruently. In order to further verify that Pb$_2$CuB$_2$O$_6$ melts congruently, 2 g of Pb$_2$CuB$_2$O$_6$ powder was heated to 1173 K, and rapidly cooled to room temperature. Analysis of the X-ray powder diffraction pattern of the melt revealed only the peaks attributable to Pb$_2$CuB$_2$O$_6$, which further demonstrates that Pb$_2$CuB$_2$O$_6$ is a congruently melting compound. No weight loss could be observed in thermogravimetrical measurement between room temperature and 1173 K.

4.2. Vibrational spectroscopic characterization

Fig. 4 shows the section from 400 to 4000 cm$^{-1}$ of the infrared spectrum of Pb$_2$CuB$_2$O$_6$. The observed frequencies between the 1150 and 1400 cm$^{-1}$ correspond to the stretching frequencies of coordinated BO$_3$ groups and the absorption peaks below 810 cm$^{-1}$, are typical for triangular BO$_3$ groups [30–32].

4.3. Magnetic susceptibility

The magnetic susceptibility and inverse susceptibility of Pb$_2$CuB$_2$O$_6$ as a function of temperature is plotted in Fig. 5. In this figure, the susceptibility has been defined as the ratio of the magnetization $M$ to the applied field $H$ ($\chi = M/H$). As shown in Fig. 5, the overall shape of the magnetic susceptibility curve from 2 to 300 K indicated paramagnetic behavior $\chi(T) = C/(T - \theta)$. The fitting parameters found are the Curie constant,
Fig. 2. The structural connectivity along each of the crystallographic axes. The blue balls are Pb, the red balls are Cu, the yellow balls are B, the green balls represent O atoms. (a) Layer of interconnected rectangular planar CuO$_4$ and triangular planar BO$_3$ groups viewed along the $a$-axis. (b) Crystal structure of Pb$_2$CuB$_2$O$_6$ viewed along the $c$-axis. (c) Crystal structure of Pb$_2$CuB$_2$O$_6$ viewed along the $b$-axis.
$C = 0.3791$ emu K/mol, and the Weiss constant, $\theta = -1.384$ K. The inset of Fig. 5 shows the linear temperature dependence of the reciprocal susceptibility, $\chi^{-1}(T)$, for Pb$_2$CuB$_2$O$_6$ fitted to the Curie–Weiss law. Using the equation $C = N\mu^2_{\text{eff}}/(3k_B)$, the Curie–Weiss constant can be related to the effective magnetic moment, where $k_B$ is the Boltzmann constant; $\mu_{\text{eff}}$ the effective magnetic moment (in Bohr magneton, $\mu_B$, units), and $N$ is the number of magnetic atoms per unit sample mass. A value of $\mu_{\text{eff}} = 1.741 \mu_B$ is obtained for the effective magnetic moment of Cu in Pb$_2$CuB$_2$O$_6$ per formula unit from the equation $C = n\mu^2_{\text{eff}}/(3k_B)$. The experimental magnetic moment is in good agreement with the free-ion value of Cu$^{2+}$ (3d$^9$ configuration) according to $\mu_{\text{eff}} = g[S(S + 1)]^{1/2} = 1.732$ with $g = 2$ and $S = 1/2$.

Table 4
Bond valence analysis of the Pb$_2$CuB$_2$O$_6$ $^{a,b}$

<table>
<thead>
<tr>
<th>Atom</th>
<th>O1</th>
<th>O2</th>
<th>O3</th>
<th>$\sum_{\text{cations}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pb</td>
<td>0.465 + 0.121 + 0.377</td>
<td>0.248 + 0.159</td>
<td>0.169 + 0.404</td>
<td>1.943</td>
</tr>
<tr>
<td>Cu</td>
<td>0.486$^{\pm 0.21}$</td>
<td>0.512$^{\pm 0.21}$</td>
<td></td>
<td>1.996</td>
</tr>
<tr>
<td>B</td>
<td>0.958</td>
<td>1.022</td>
<td>0.942</td>
<td>2.922</td>
</tr>
<tr>
<td>$\sum_{\text{anions}}$</td>
<td>1.921</td>
<td>1.915</td>
<td></td>
<td>2.027</td>
</tr>
</tbody>
</table>

$^a$ Bond valences calculated with the program Bond Valence Calculator Version 2.00, Hormillosa, C., Healy, S., Stephen, T. McMaster University (1993).

$^b$ Valence sums calculated with the formula: $S_i = \exp[(R_0 - R_i)/B]$, where $S_i$ = valence of bond “i” and $B = 0.37$. Right superscripts indicate the number of equivalent bonds for cations.

Fig. 3. The DTA of Pb$_2$CuB$_2$O$_6$ compound.

Fig. 4. The mid-infrared spectra of Pb$_2$CuB$_2$O$_6$. 
The negative value for the Weiss constant $\theta = -1.384$ K implies the possible existence of antiferromagnetism in the $\text{Pb}_2\text{CuB}_2\text{O}_6$ sample at lower temperatures. Further susceptibility experimentation incorporating a dilution refrigerator would answer this question.

This material represents another in a series of copper containing borates, phosphates, and molybdates that have been investigated for their magnetic properties $[14–16,33–35]$. The magnetic properties can be easily modeled by Heisenberg magnetism (typically 1D chains and especially dimers). These materials have magnetic ordering transitions under 100 K (some are ferromagnetic [FM] and others are antiferromagnetic [AFM]) and they illuminate exchange interaction strengths and selection rules for how electrons choose exchange pathways.

Referring to Fig. 2b, the copper atoms constitute a rectangular 2D lattice when viewed along the $c$-axis and from Fig. 2c the copper atoms form a parallelogram 2D lattice when viewed along the $b$-axis. From these symmetries one would expect measurable magnetic ordering within the temperature range observed; however the 2D symmetry in Fig. 2a (when the crystal is viewed along the $a$-axis) is practically hexagonal. It is well known that hexagonal spin lattices are frustrated instead of anti-ferromagnetic and this observation (coupled with the negative tendency of the Weiss constant) may explain the lack of magnetic ordering at $T > 2$ K.

$\text{Pb}_2\text{Cu(BO}_3\text{)}_2$ is interesting because exchange and magnetic dipole interactions appear to completely cancel leaving essentially only paramagnetism. The absence of magnetic order might have interesting implications about the electron exchange integral in this class of compounds. Therefore this compound can serve as the ‘zero’ case for this class of materials and might link the AFM data to the FM data thus forming a complete model. Particularly, magnetic moment experiments at milli-Kelvin temperatures might observe an anti-ferromagnetic transition and the particular transition temperature would represent the relative spin exchange energies along the horizontal versus (two equivalent) diagonal directions in Fig. 2a. Should this happen to be the case, it would help explain how these materials decide whether to be FM or AFM.

5. Conclusions

$\text{Pb}_2\text{CuB}_2\text{O}_6$ crystals have been grown successfully by slow cooling and the crystal structure has been determined. The main structural elements are sheets of isolated CuO$_4$ square planes that are rotated out of the $b$–$c$ plane and connected by BO$_3$ and PbO$_7$ units. $\text{Pb}_2\text{CuB}_2\text{O}_6$ is a congruently melting compound. The temperature dependences of the susceptibility shows that $\text{Pb}_2\text{CuB}_2\text{O}_6$ exhibits paramagnetic behavior above 2 K and the $\chi - T$ curve fits the Curie–Weiss law $\chi(T) = C/(T - \theta)$. The absence of magnetic ordering separates this compound from others with similar crystal chemistry and might serve to link ferromagnetism to antiferromagnetism in this class of materials.

Acknowledgements

We gratefully acknowledge the support from the National Science Foundation (Solid State Chemistry Award No. DMR-0312136), the EMSI program of the National Science Foundation at the Northwestern University Institute for Environmental Catalysis (Grant No. 9810378), and the Department of Energy, BES-Chemical Sciences, Geosciences, and Biosciences Division under grant No. DE-FG0203ER15457 for support of this work, and the use of the Central
Facilities supported by the MRSEC program of the National Science Foundation (DMR-0076097) at the Materials Research Center of Northwestern University.

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